

Professor: J.D. WilsonValue: 10%

Instructions: All questions have equal value. Answers should be stated with two decimal point precision, and in identified SI units (e.g. 20.02°C , 278.16 K , 1.09 kg m^{-3}). Please document your working tidily — there is potentially a one mark penalty for illegible or unintelligible working. Please drop off your assignment (labelled with your name and ID number) in the drop-off box outside Tory 3-40. A two mark penalty will be applied for late assignments received before noon Thursday 15 Oct. After that time, the late penalty will be five marks.

Task: Add together the last five digits of your student I.D. number, to form what we shall interpret as a ground-level temperature T_1 : e.g. I.D. number 1198765 $\rightarrow T_1 = 35^{\circ}\text{C}$. Then:

1. Assuming the emissivity of the ground surface is $\epsilon = 0.95$, compute the emitted longwave radiative flux density $L \uparrow$ corresponding to ground temperature T_1 .
2. Assuming ground-level pressure is $P_1 = 930\text{ hPa}$, compute the air density ρ_1 implied by this combination (P_1, T_1) .
3. Adopt the hydrostatic law, evaluating the right hand side as $-\rho_1 g$, to compute the vertical distance Δz between the ground and the 850 hPa surface (i.e. the altitude where pressure is $P_2 = 850\text{ hPa}$).
4. Assuming the temperature variation from ground to the P_2 level follows the dry adiabatic lapse rate (DALR), compute the temperature T_2 (in Celcius units) at this level.
5. Compute the density ρ_2 of air whose state is defined by (P_2, T_2) .

Data

- $1\text{ hPa} = 100\text{ Pa}$, $T\text{ [K]} = T\text{ [}^{\circ}\text{C]} + 273.16$

- $\frac{\Delta P}{\Delta z} = -\rho g$

The hydrostatic law. ΔP [Pascals], the change in pressure as one ascends a distance Δz [m]; ρ [kg m^{-3}] the air density; $g = 9.81\text{ [m s}^{-2}\text{]}$ acceleration due to gravity.

- $P = \rho R T$

The ideal gas law. P [Pascals], pressure; ρ , [kg m^{-3}] the density; T [Kelvin], the temperature; and $R = 287\text{ [J kg}^{-1}\text{ K}^{-1}\text{]}$, the specific gas constant for air.

- $L \uparrow = \epsilon \sigma T^4$

Stefan-Boltzmann law. $L \uparrow$ [W m^{-2}], the emitted longwave energy flux density; ϵ , the emissivity of the surface (dimensionless); $\sigma = 5.67 \times 10^{-8}\text{ [W m}^{-2}\text{ K}^{-4}\text{]}$, the Stefan-Boltzmann constant; T [K], the surface temperature.

- $\frac{\Delta T}{\Delta z} = -0.01\text{ [K m}^{-1}\text{]}$

The dry adiabatic lapse rate (DALR), i.e. for every one metre of ascent the temperature decreases by 0.01 degrees Kelvin. (Note that a *change* of one degree Kelvin is the same as a *change* of one degree Celcius).