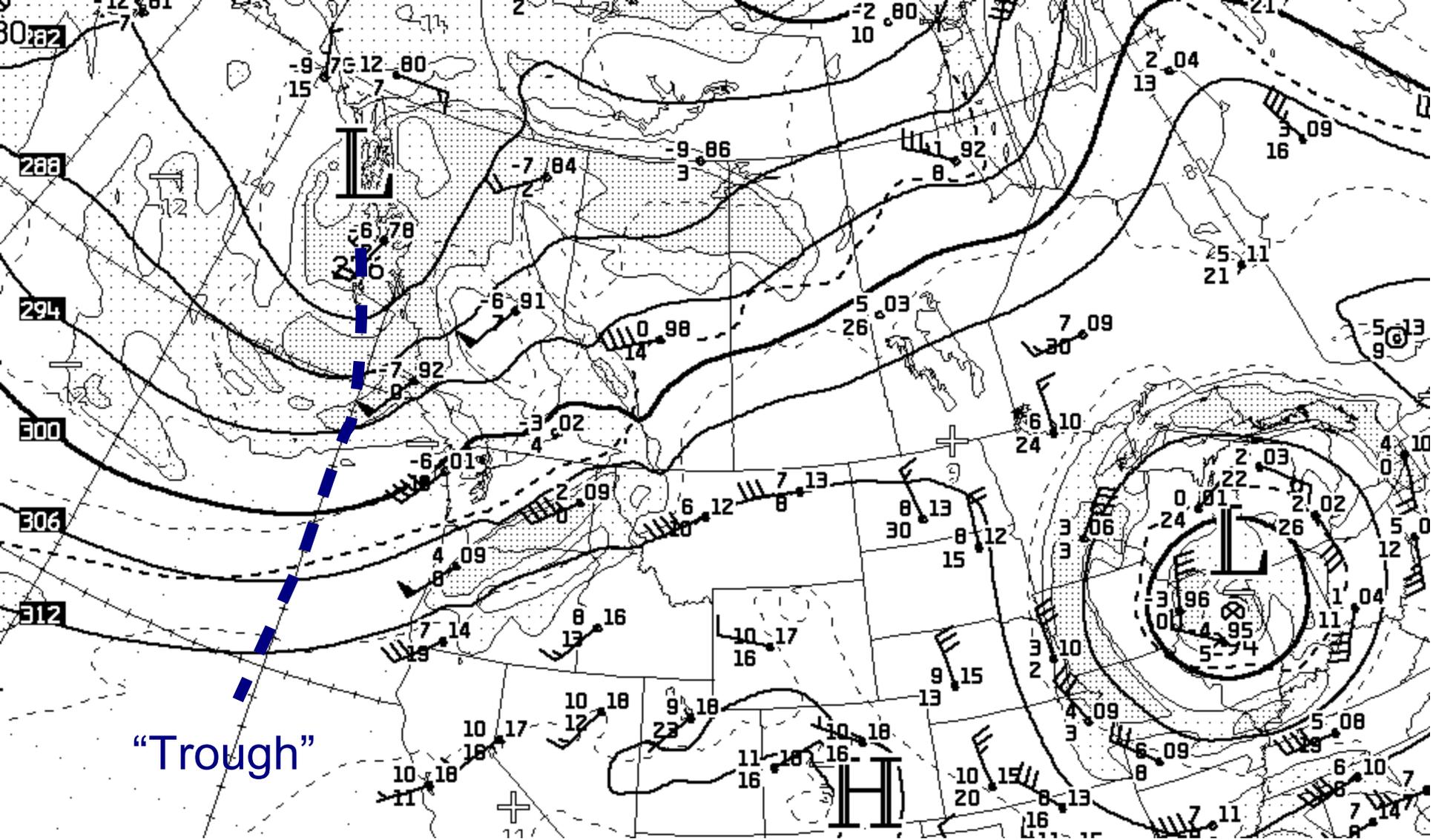


## Complete Ch 3 – still to cover – influences on temperature on larger scales

- A global energy budget and “Earth’s Equilibrium Temperature” (Section 3-2, p75)
- Latitudinal variability in net radiative forcing
- Other geographic influences (sea/land, elevation...)

## Begin Ch 4 – Atmospheric Pressure and Wind



- solid lines, height contours
- dashed lines isotherms
- heavy stippling,  $T - T_d \leq 2^\circ\text{C}$
- notice wind blows parallel to the height contours

MSC 700 hPa analysis, valid 12Z Tues 27 Sept. 2011

Why might we consider earth's global climatological temperature  $T_{eq}$  to be at equilibrium (Sec. 3-2)?

Because there is a stabilizing feedback. Let  $\Delta T_{eq}$  be the change in  $T_{eq}$  over time interval  $\Delta t$ . Then,

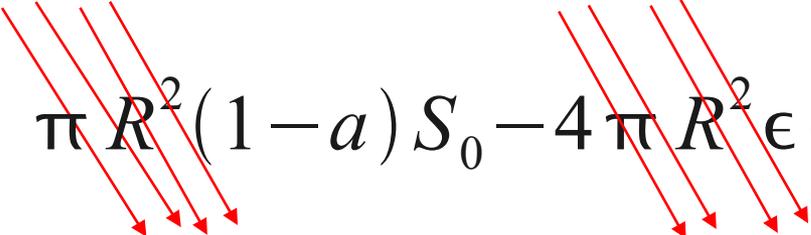
$$\frac{\Delta T_{eq}}{\Delta t} \propto \underbrace{\pi R^2}_{\text{area of earth's shadow}} (1-a) S_0 - \underbrace{4\pi R^2}_{\text{area of earth's surface}} \epsilon \sigma T_{eq}^4$$

Rate of change  $\propto$  gains          minus          losses

$R$  is earth's radius,  $S_0$  is the solar constant,  $a$  ( $\approx 0.3$ ) is the planetary albedo,  $\epsilon$  ( $\approx 1$ ) is the planetary emissivity and  $\sigma$  is the Stefan-Boltzmann constant. The proportionality constant involves the heat capacity of the earth-atmosphere system. (In reality  $a, \epsilon$  may depend on  $T_{eq}$ ).

At earth's (hypothetical) equilibrium temperature, there is balance:

Both sides of the equation are zero, thus setting the right hand side to zero

$$C \frac{\Delta T_{eq}}{\Delta t} = 0 \propto \pi R^2 (1-a) S_0 - 4\pi R^2 \epsilon \sigma T_{eq}^4$$


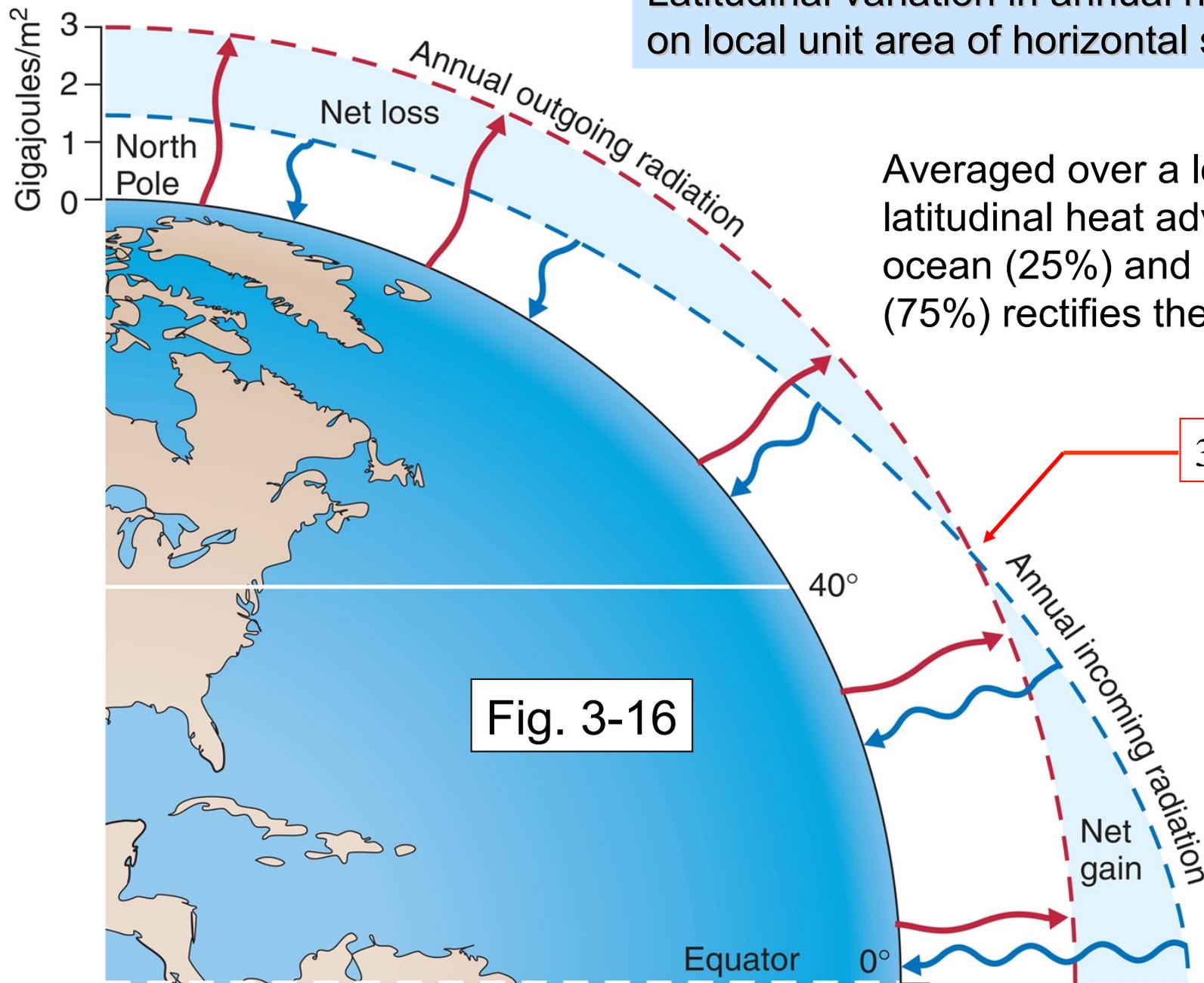
Common factors cancel

Set  $a = 0.3$  and  $\epsilon = 1$  to obtain earth's (radiative) equilibrium temperature (Sec. 3-2),

$$T_{eq} = 255 \text{ K}$$

(However this entirely neglects the effect of the atmosphere – true global-annual mean surface temperature is about **288 K**)

# Latitudinal variation in annual net radiation on local unit area of horizontal surface

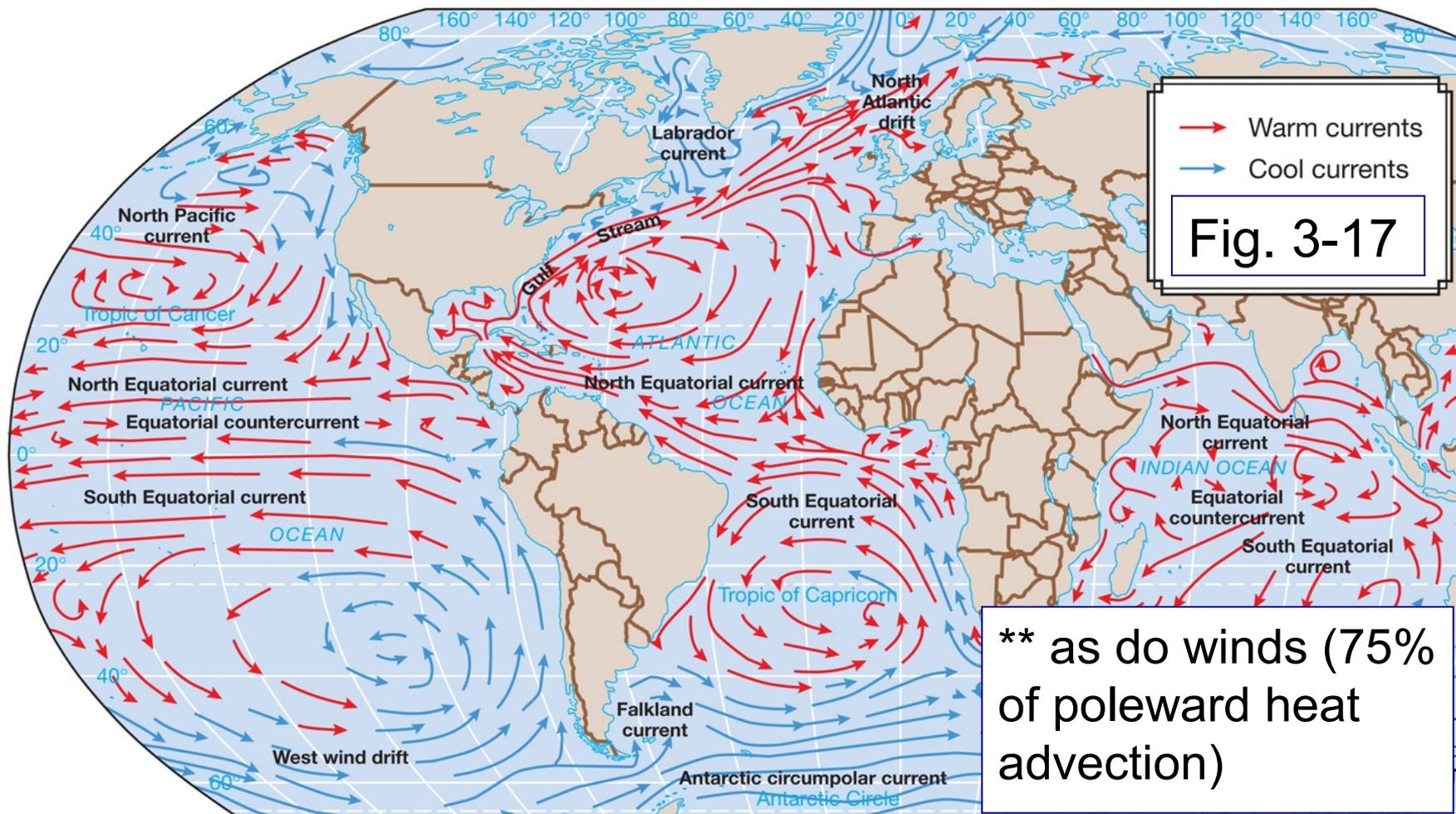


Averaged over a long period, latitudinal heat advection by ocean (25%) and atmosphere (75%) rectifies the imbalance

Fig. 3-16

# Global Temperature Distribution – factors controlling temperature on regional & global time & space scales

- Latitude – modulates solar radiation (solar elev., daylength)
- Distribution of land & water – ocean currents advect heat\*\*



# Global Temperature Distribution – factors controlling temperature on regional & global time & space scales

- Distribution of land & water
  - surface thermal inertia, surface energy balance



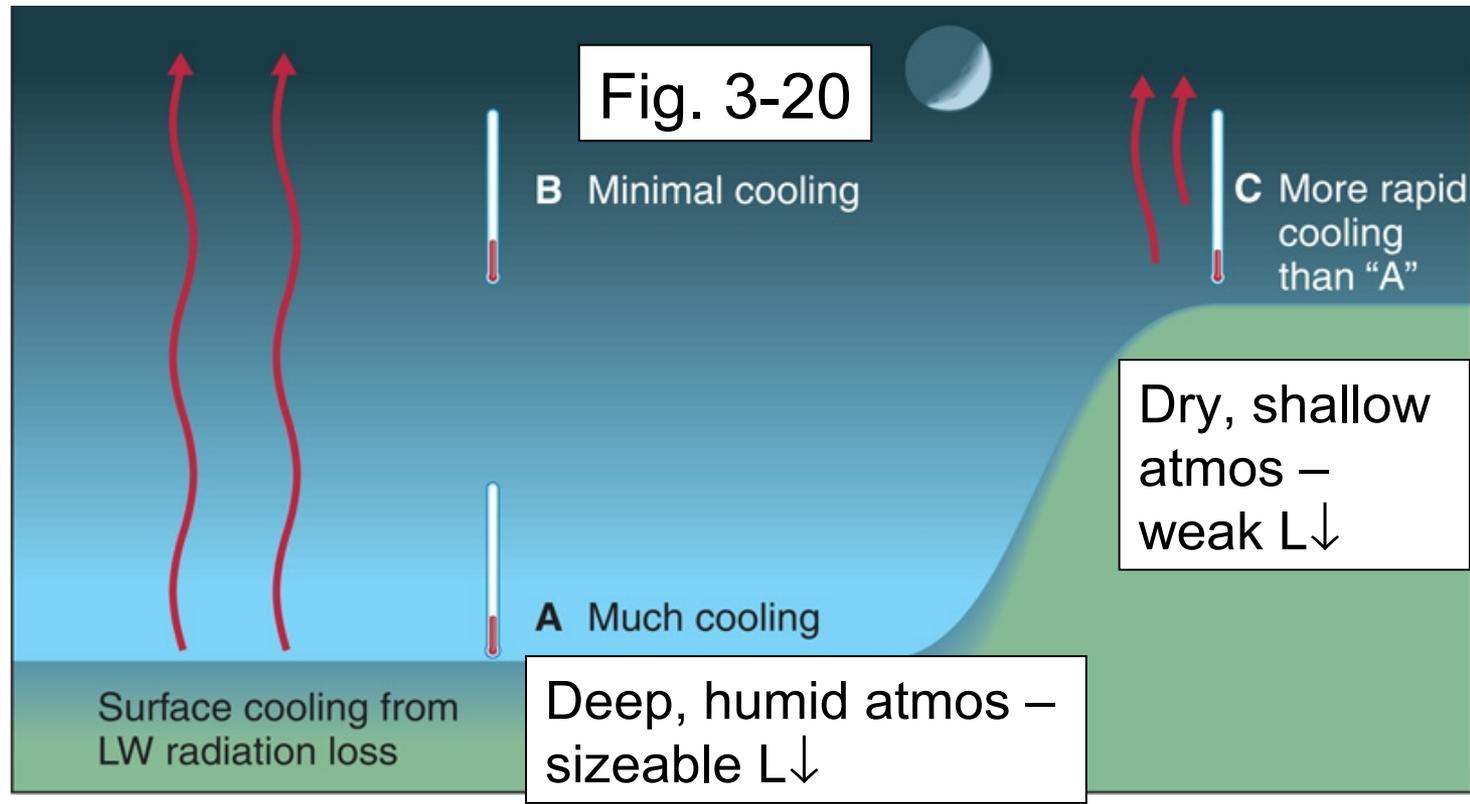
Why are water bodies “more conservative” (p78) in their temperature?

- solar radiation penetrates to some depth, so warms a volume
- much of available radiant energy used to evaporate water (  $Q_E$  )
- mixing of the water in the ocean/lake “mixed layer” ensures heat is deposited/drawn from a deep layer
- water has a higher specific heat capacity ( $4128 \text{ J kg}^{-1} \text{ K}^{-1}$ ) than unsaturated soils (e.g. soil minerals  $\sim 1000 \text{ J kg}^{-1} \text{ K}^{-1}$ )

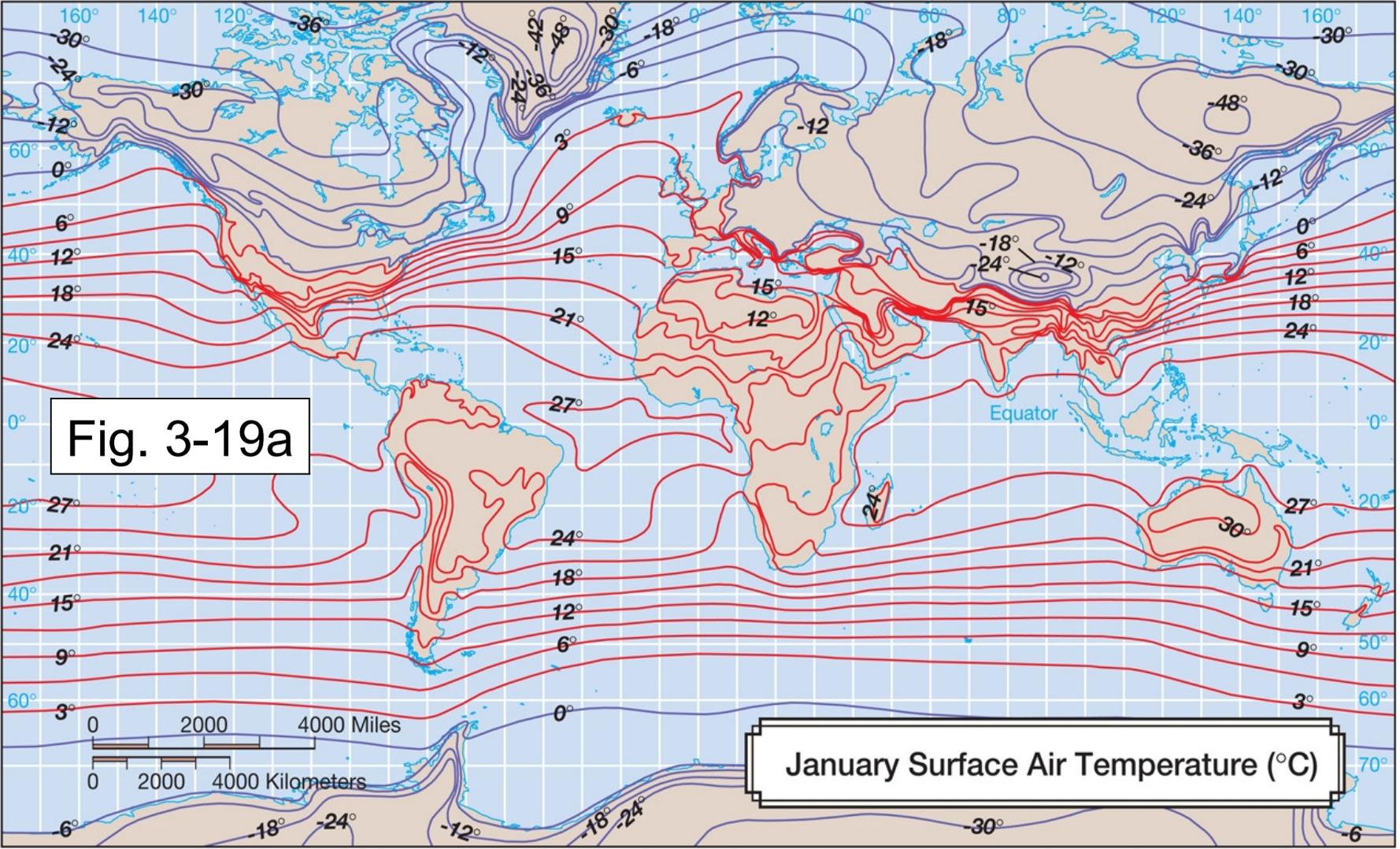
# Global Temperature Distribution – factors controlling temperature on regional & global time & space scales

- Distribution of land & water
- Topographic steering/blockage of winds  
e.g. isolation of winter continental interior from warmer ocean by intervening mountain range blocking advection by wind; mountain range extracts precipitation (rain shadow)... etc.

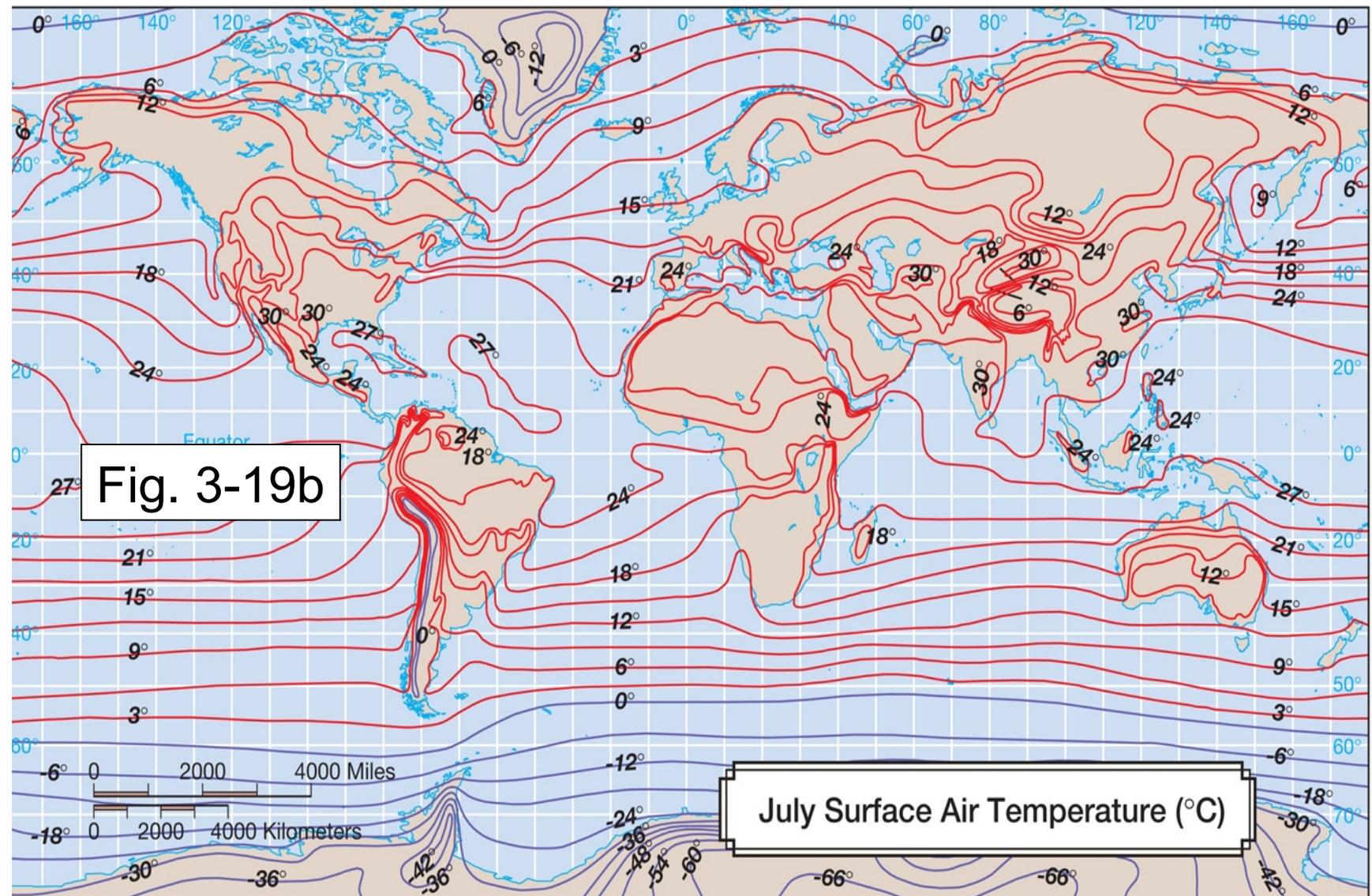
## Elevation & slope of terrain



- latitudinal temperature gradient is strongest in the winter hemisphere (during high lat. summer the lower midday sun is offset by long daylength)
- in summer (winter) temperature over continent is warmer (cooler) than over ocean (influence of latent heat flux in energy balance)



- northern hemisphere has a steeper winter latitudinal temperature gradient than the southern hemisphere (much greater proportion of ocean than land)



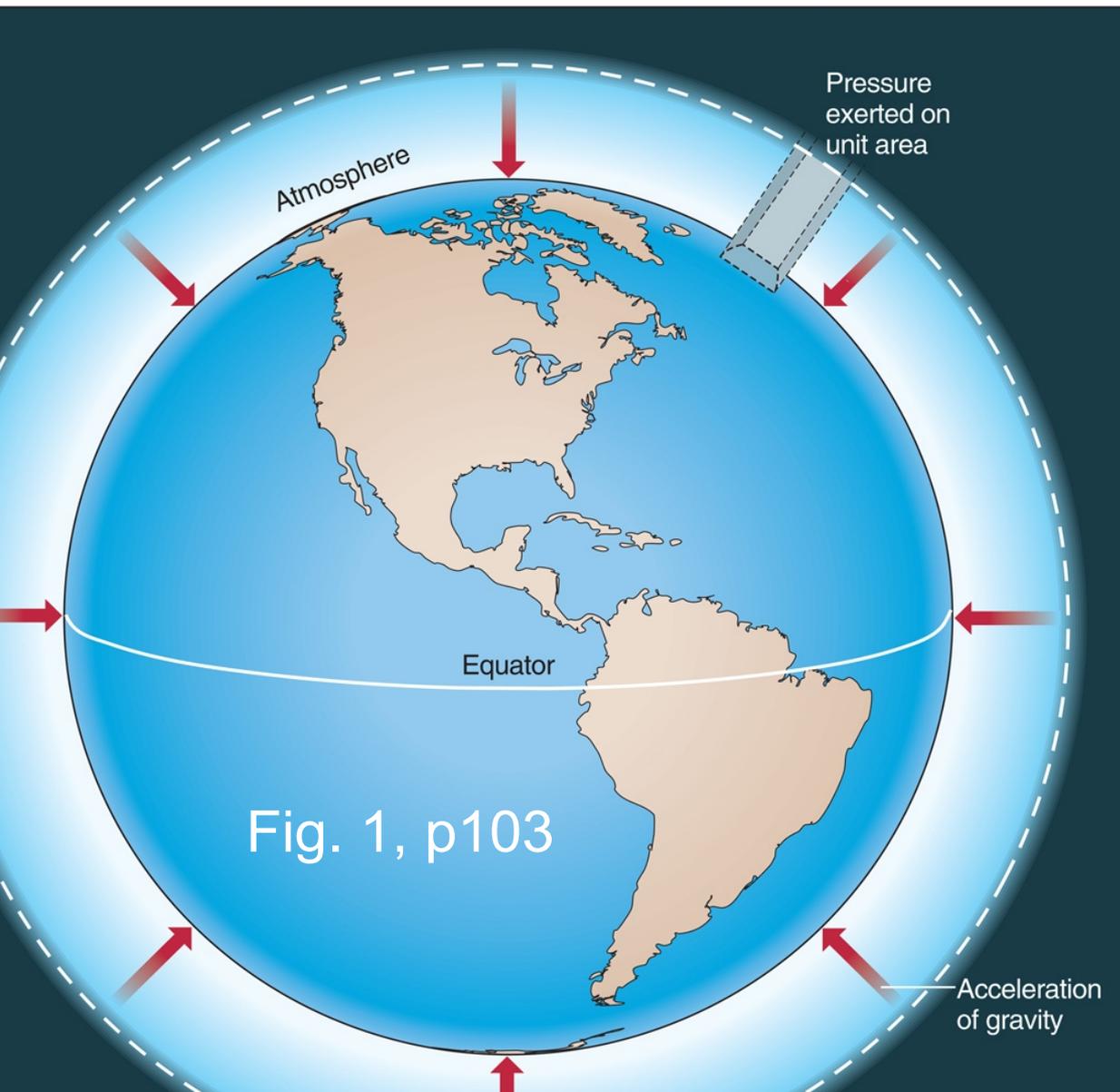
## Ch. 4 Atmospheric Pressure and Wind

- we've covered some concepts from Ch4 already – e.g. definition and units of pressure, the cause of its height variation, its control over wind
- now we need a more quantitative view of the statics and the dynamics (forces and their balance) of the atmosphere. (Setup for Assignment 1)
- we'll begin by looking in more detail at hydrostatic pressure variation in the vertical
- next focus on *horizontal* pressure gradients and learn to think instead of the corresponding “height gradients”
- then cover the theoretical relationship between wind speed and the height gradient



Sir Isaac Newton  
1642 - 1727

In the macroscopic view, pressure at the base of a static air column is controlled by overlying mass



$$p = \frac{M g}{A}$$

- But simultaneously, there is a valid microscopic view – the pressure at every point is related to the temperature and density at that point...

$$p = \rho R T$$

$p$  , pressure [Pa]

$\rho$  , density [kg m<sup>-3</sup>]

$R$  , 287 [J kg<sup>-1</sup> K<sup>-1</sup>] , specific gas const. for dry air

$T$  , temperature [K]

*Convert pressure to Pascals and temperature to Kelvin, for use in this equation*

Question: these paragliders are flying at a height of 1000 m above sea-level. A pilot's instrument reports

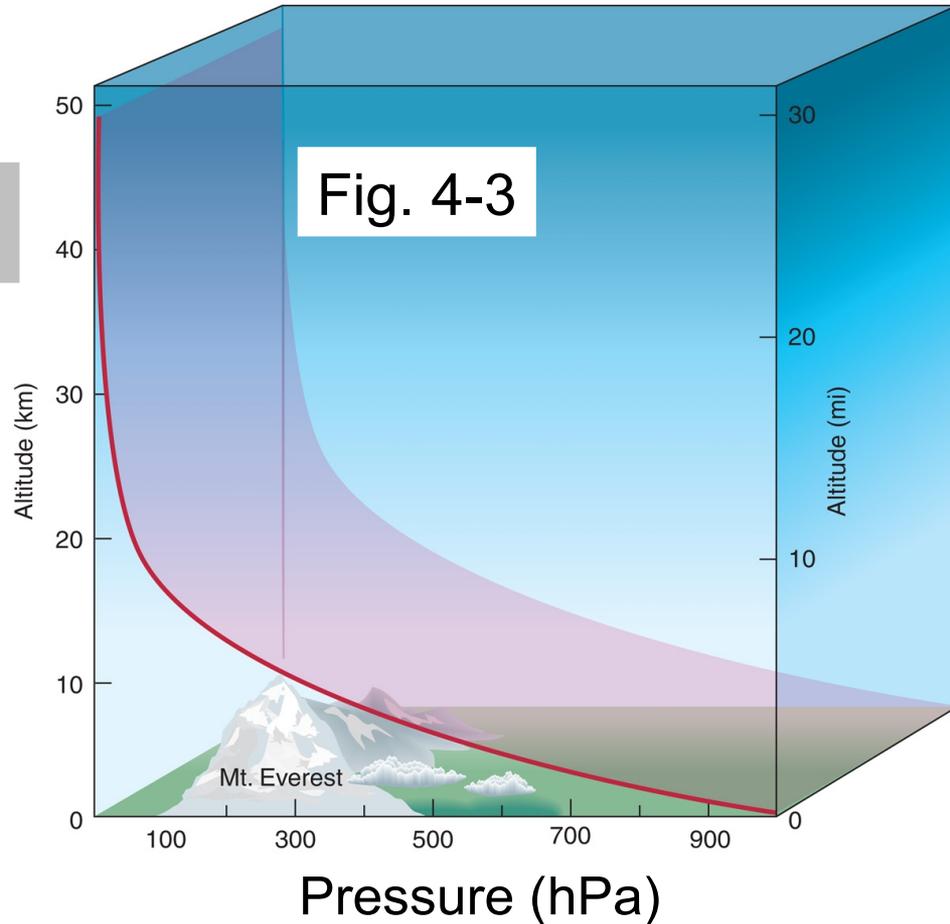
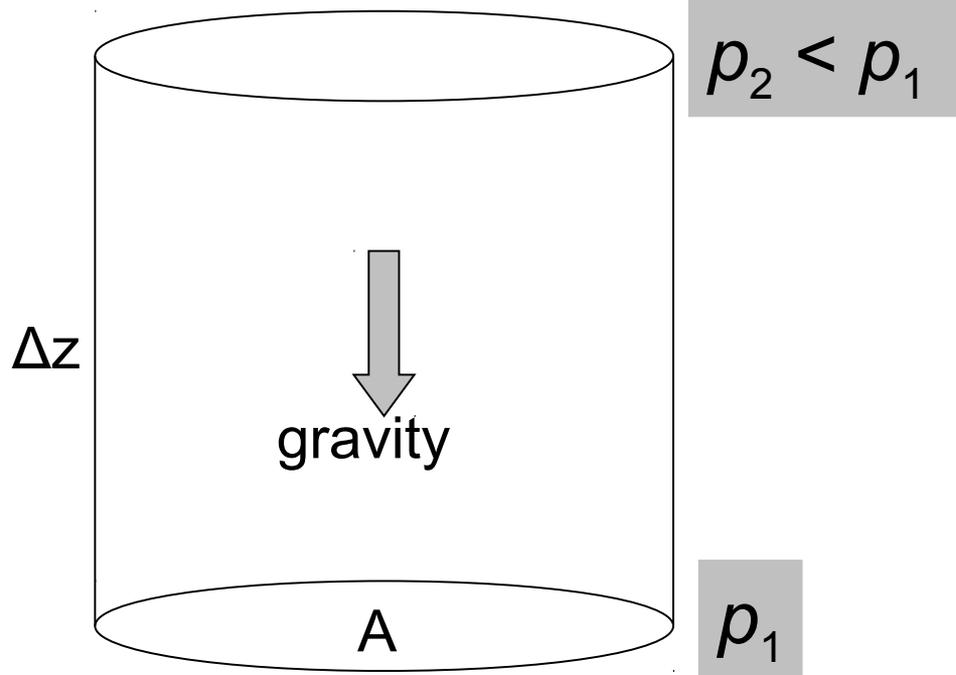
$$p = 900 [\text{hPa}],$$
$$T = 25 [^{\circ}\text{C}].$$

The air density at flight level is?

$$\rho = \frac{p}{R T} = \frac{90000}{287 \times (273.15 + 25)} =$$



# Local hydrostatic equilibrium (Sec. 4-3, p112)



- gravity pulls down
- pressure pushes up harder than down
- introducing area  $A$  and depth  $\Delta z$  of column, result of a force balance is:

## The hydrostatic equation (Sec. 4-3, p112)

Gives the change in pressure ( $\Delta p$ ) associated with an increase ( $\Delta z$ ) in height

$$\frac{\Delta p}{\Delta z} = - \rho g \left[ \frac{\text{Pa}}{\text{m}} \text{ or } \text{Pa m}^{-1} \right]$$

$\rho$  = air density [ kg m<sup>-3</sup> ] (approximately 1, near ground)  
 $g$  = grav. accel'n = 9.81 [ m s<sup>-2</sup> ] (approximately 10)

**Thus:** near ground, pressure increases by an amount  $\Delta p = - 10 \text{ Pa}$  for each 1 m increase in height

100 Pa (= 1 hPa) per 10m  
100 hPa per 1 km

**Question: if those paragliders descend 100 m, estimate the pressure at their new flight level:**

$$p_1, T_1 \text{ (known)} \quad \rightarrow \quad p_2, T_2$$

$$p_1 = 900 \text{ hPa,}$$

$$T_1 = 25^\circ \text{C}$$



## Importance of the hydrostatic equation:

- although the atmosphere obviously is not static, it turns out that in the real atmosphere variation of pressure with height is closely approximated by the hydrostatic equation – particularly if we consider the pressure (and related properties) to have been averaged on horizontal planes over areas of order 100 km x 100 km (the “synoptic scale” view). Most Numerical Weather Prediction (NWP) models and all Dynamical Climate models (GCM’s) treat the pressure distribution as hydrostatic – a big simplification to the vertical force balance
- next, as a precursor to considering the balance of horizontal forces, let's consider horizontal pressure gradients... their cause, and their representation as “height gradients”